Reduction of Influence of Variation in Center Frequencies of RF Echoes on Estimation of Artery-Wall Strain

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Abstract—Atherosclerotic change of the arterial wall leads to a significant change in its elasticity. For assessment of elasticity, measurement of arterial wall deformation is required. For motion estimation, correlation techniques are widely used, and we have developed a phase-sensitive correlation method, namely, the phased-tracking method, to measure the regional strain of the arterial wall due to the heartbeat. Although phase-sensitive methods using demodulated complex signals require less computation in comparison with methods using the correlation between RF signals or iterative methods, the displacement estimated by such phase-sensitive methods are biased when the center frequency of the RF echo apparently varies. One of the reasons for the apparent change in the center frequency would be the interference of echoes from scatterers within the wall. In the present study, a method was introduced to reduce the influence of variation in the center frequencies of RF echoes on the estimation of the artery-wall strain when using the phase-sensitive correlation technique. The improvement in the strain estimation by the proposed method was validated using a phantom. The error from the theoretical strain profile and the standard deviation in strain estimated by the proposed method were 12.0% and 14.1%, respectively, significantly smaller than those (23.7% and 46.2%) obtained by the conventional phase-sensitive correlation method. Furthermore, in the preliminary in vitro experimental results, the strain distribution of the arterial wall well corresponded with pathology, i.e., the region with calcified tissue showed very small strain, and the region almost homogeneously composed of smooth muscle and collagen showed relatively larger strain and clear strain decay with respect to the radial distance from the lumen.

I. INTRODUCTION

Pathological change of the arterial wall due to atherosclerosis leads to a significant change in its mechanical properties [1], [2]. Most conventional methods for noninvasive measurement of elasticity are based on measurement of the pulse wave velocity (PWV) [3]–[6] or that of the change in diameter [7]–[10]. Although these methods are useful in terms of their ability to assess the vascular elasticity noninvasively, the spatial resolution in elasticity measurement is limited to the propagating distance of the pulse wave or the entire circumference.

Elastography was introduced by Ophir et al. to measure the strain distribution of biological tissue by cross-correlating 2 RF signals before and after deformation [11]–[14]. Elastography was applied to strain imaging of the arterial wall with intravascular ultrasonography (IVUS), namely, intravascular elastography [15], [16]. In the cited studies, the elasticity distribution of coronary atherosclerotic plaque was obtained by the measured displacement distribution in the radial direction. This measured elasticity distribution was compared with the pathological image, and the results suggested the potential for tissue characterization of atherosclerotic plaque by measurement of its elasticity.

As a transcutaneous approach, the displacement and strain around carotid atherosclerotic plaque during one cardiac cycle have been measured using tissue Doppler imaging [17]. The inhomogeneity of displacements measured upstream and downstream of atherosclerotic plaque suggests that artery-wall motion has potential for use in the evaluation of plaque vulnerability. Furthermore, some research studies on noninvasive vascular elastography have been conducted [18]–[20]. In most of the above-mentioned methods, a correlation-based technique is used for the estimation of the displacement and strain of the arterial wall [15]–[18], [21]. Also, in recent years, iterative methods have been introduced for estimating 2-D displacement [19], [22].

We have been studying the measurement of the displacement and radial strain (change in thickness) of the arterial wall based on the phase-sensitive correlation technique and have developed the phased-tracking method [23]–[27]. Elasticity images of the human carotid artery have been obtained based on the measured strain distribution, and the potential for transcutaneous tissue characterization has been shown by classification of elasticity images using elasticity reference data obtained by in vitro experiments [28]–[31].

The phase-sensitive correlation method using a demodulated complex signal, which was first introduced by Kasai et al. for blood flow measurement [32], requires less computation in comparison with the cross-correlation between RF signals. Methods based on the cross-correlation between RF signals can estimate displacement larger than half of the wavelength of ultrasound, but such estimation requires calculation of correlation functions at multiple lags between RF signals in 2 frames. On the other hand, phase-sensitive correlation methods estimate displacement less than half of the wavelength, but require calculation of
only one complex correlation function at no lag between
demodulated complex signals in 2 frames. The displace-
ment of an object can be estimated using phase-sensi-
tive methods by keeping the frame rate sufficiently high
so that the displacement between 2 frames becomes less
than half of the wavelength of ultrasound. However, the
displacements estimated by phase-sensitive methods are
biased when the center frequency of the RF echo appar-
ently varies. One of the reasons for the apparent change in
center frequency would be the interference of echoes from
scatterers within the wall. The center frequency could be
apparently changed depending on the scatterer spacing.

Konofagou et al. proposed a method to estimate tissue
strain from the shift of the centroids in power spectra of
RF echoes by assuming that the change in center frequen-
cy is proportional to the magnitude of strain. As described
in [33], [34], this method is robust when the decorrelation
of RF signals in 2 different frames is significant due to a
large strain of up to 10% between frames. However, the
accuracy of this method is worse than those of methods
based on cross-correlation of RF signals when the signal
correlation is assured.

In methods based on the cross-correlation of RF sig-
als in 2 frames, companding, termed temporal stretch-
ing, is applied to the RF signals before correlating them
to compensate for the change in center frequency distri-
butions between 2 frames (called scaling) [12], [35]–[42].
Such difference between the center frequency distributions
in 2 frames is not negligible when the strain that arises
between 2 frames is large because a large deformation sig-
nificantly changes the spacing of scatterers. Although the
center frequency “difference” between 2 frames is compen-
sated by companding, the center frequency distributions
themselves are not spatially homogeneous, even after the
application of companding. Nevertheless, such methods
yield unbiased displacement estimates by compensating
for only the center frequency difference between 2 frames
[21] because the displacement estimation by the cross-cor-
relation between RF signals does not require knowledge of
the center frequency. However, as described in [21], such
methods require considerable computation because both
the scale factor in companding and time delay between
RF signals must be determined.

In the phase-sensitive correlation-based methods, a sub-
sample small displacement between 2 consecutive frames
is estimated using the phase of the complex correlation
function. In these methods, the center frequency distribu-
tions in 2 consecutive frames are assumed to be the same
when the frame rate is sufficiently high and the deforma-
tion between 2 consecutive frames is small. Therefore,
companding is not applied. However, knowledge of the
center frequency at each location is necessary to obtain
an unbiased displacement estimate using the phase of the
complex correlation function. Although Loupas et al. pro-
posed a method for estimating the center frequency distri-
bution by correlation of the demodulated complex signals
[43], [44], center frequency distributions in 2 frames are
still assumed to be the same.

In this study, a new method using the phase-sensitive
estimation technique, which does not require the assump-
tion that center frequency distributions in 2 different
frames are the same, was examined with the aim of reduc-
ing the influence of center frequency variation on the esti-
mation of artery-wall strain. The improvement of accuracy
by the proposed method was validated using a cylindrical
phantom. Furthermore, preliminary in vitro experimental
results were obtained and are herein presented.

II. PRINCIPLES

A. Conventional Phase-Sensitive Correlation Method for
Estimating Displacement Distribution in the Arterial Wall

The ultrasonic beam scans \( I (= 46 \) in this study) posi-
tions along the longitudinal direction of the artery. As
shown in Fig. 1, with respect to each beam position \( i ( =
1,2, \ldots, I ) \), RF pulses are transmitted with a time interval
\( T \) from an ultrasonic probe, and the echo reflected by
the arterial wall is received by the same probe. By referring
to a B-mode or M-mode image constructed based on the re-
ceived RF echoes, the depths, \( x_i(0) \) and \( x_{M,T}(0) \) corre-
sponding to the distances from the probe), of the lumen-
intima and media-adventitia boundaries of the posterior
wall are manually assigned in the initial frame, where \( MT \)
is the number of sampled points between these assigned
boundaries. Depth \( x_m(n) \) at the \( m \)-th sampled points \( ( m
= 1,2, \ldots, MT ) \) in the \( n \)-th frame is defined as follows:

\[
x_m(n) = x_i(0) + (m - 1) \cdot \Delta X, \quad (m = 1,2,\ldots, MT) (1)
\]

where \( \Delta X = c_0 / (2f_s) \) (\( f_s \): sampling frequency) is the inter-
val of sampled points in the direction of depth. After depths
\( x_i(0) \) and \( x_{M,T}(0) \) in the initial frame \( n = 0 \) are
manually assigned, the displacements \( \{ u_m(n) \} \)
\( (m = 1,2,\ldots,MT) \) at multiple points along an ultrasonic beam
are obtained by estimating the instantaneous displace-
ment, \( \{ \Delta u_m(n) \} \), between \( n \)-th and \( (n + 1) \)-th frames \( (n
= 0,1,2,\ldots,N) \) at the respective points \( m = 1,2,\ldots,MT \) as
described below.

Let us define the RF signal at depth \( x \) and beam posi-
tion \( i \) in the \( n \)-th frame by \( s_i(n;x) \). The instantaneous displace-
ment, \( \Delta u_m(n) \), at \( x_m(n) \) between the \( n \)-th and \( (n + 1) \)
th frames (corresponding to the average velocity between
2 frames) is estimated based on the time delay, \( \Delta \tau_m(n) \),
between RF signals, \( s_i(n;x) \) and \( s_i(n+1;x) \), at \( x = x_m(n) \)
because displacement \( \Delta u_m(n) \) between the \( n \)-th and \( (n + 1) \)-th frames is expressed by \( \Delta u_m(n) = c_0 \Delta \tau_m(n) / 2 \),
where \( c_0 \) is the speed of sound [23], [32]. Time delay \( \Delta \tau_m(n) \)
at the \( n \)-th sampled point is related to the phase change
\( \Delta \theta_m(n) \) of \( s_i(n+1;x) \) from \( s_i(n;x) \) as follows:

\[
\Delta \tau_m(n) = \frac{\Delta \theta_m(n)}{2\pi f_{cm}(n)}, \quad (2)
\]
where \( f_{c,m}(n) \) is the center frequency of the RF echo at depth \( x_{m}(n) \) in the \( n \)th frame. As described in Section II-B, center frequency \( f_{c,m}(n) \) is not spatially constant along the ultrasonic beam and temporally varies because the frame is different. Using the quadrature demodulated signal, \( z_i(n; x) \), of \( s_i(n; x) \), phase shift \( \Delta \theta_m(n) \) between 2 frames at depth \( x_{m}(n) \) can be estimated by the complex correlation \( r_{m,n}(m',n') \) as follows [32]:

\[
\begin{align*}
    &r_{m,n}(m',n') = \sum_{j=-I_{av}}^{I_{av}} \sum_{l=0}^{M_c-1} z^*(n; x_m(n) + l \cdot \Delta X) \\
    &\cdot z(n + n'; x_m(n) + (l + m') \cdot \Delta X),
\end{align*}
\]

where * represents the complex conjugate and \( r_{m,n}(m',n') \) defines the complex correlation function with lags, \( m' \) and \( n' \), in the directions of depth and frame, respectively. Although the correlation function is usually normalized by the average amplitude of the complex signal in the correlation window, normalization was not applied in this study because only the phase of the complex correlation function was used for estimation of the displacement. The number of sampled points in the direction of depth used for calculating correlation is defined by \( M_c \), and the correlation window extends from the \( m \)th point to the \((m + M_c - 1)\)th point because the leading edge of the echo from the point of interest (\( = m \)th points) should correspond to \( m \)th point. Phase angle \( \Delta \theta_{m,n}(0,1) \) of \( r_{m,n}(0,1) \) corresponds to the phase shift \( \Delta \theta_m(n) \) between RF echoes in 2 consecutive frames [32], where \( r_{m,n}(0,1) \) means the correlation between signals at the same depth \( (m' = 0) \) in 2 consecutive frames \( (n' = 1) \). In blood flow measurement using the complex correlation, the correlation function \( r_{m,n}(m',n') \) is temporally averaged in the direction of the frame. This can be done because the RF signals are acquired at a very high frame rate (several kHz) in the measurement of blood flow. Although the frame rate in this study (286 Hz) was higher than that in conventional B-mode imaging (at most 60 Hz), it was much lower than that in blood flow measurement, and temporal averaging in the direction of the frame was not applied in (3).

In this study, a 2-D kernel was used in calculation of the complex correlation function to reduce the variance in the estimated displacement distribution in the arterial wall. The 2-D kernel was used even when the displacement was estimated based on the conventional methods described in this section to compare the estimated displacements with those by the proposed method. The phase angle \( \Delta \theta_{m,n}(0,1) \) represents the spatially averaged phase shift of RF echoes in the correlation window consisting of \((M_c \text{ samples}) \times ((2I_{av} + 1) \text{ beam positions})\). In this study, \( I_{av} \) was set to 1 because the number \((2I_{av} + 1)\) of averaging (beam positions) is significantly increased from 1 to 3 (200% increase) when \( I_{av} \) changes from 0 to 1, but the number \((2I_{av} + 1)\) is not increased so much \((67\%: I_{av} = 1 \rightarrow 2, 40\%: I_{av} = 2 \rightarrow 3)\) when \( I_{av} \) is further increased. In addition, a larger \( I_{av} \) worsens the lateral spatial resolution.

In the conventional phase-sensitive correlation method, using the estimated phase shift, \( \Delta \theta_{m,n}(0,1) \), instantaneous displacement \( \Delta u_m(n) \) between 2 consecutive frames is obtained as follows:
\[ \Delta u_m(n) = \frac{c_0 \Delta \theta_m(n)}{4\pi f_{c,m}(n)} \approx \frac{c_0 \Delta \theta_m(n)}{4\pi f_{dem}} = \frac{c_0}{4\pi f_{dem}} \Delta r_{m,n}(0,1). \]  

(4)

In (4), knowledge of the center frequency \( f_{c,m}(n) \) is necessary to obtain an unbiased estimate. It is, however, unknown. Therefore, in conventional phase-sensitive correlation methods, the frequency of the reference sinusoid, \( f_{dem} \), in the quadrature demodulation is used as the frequency term in the denominator of (4), whereas it should be the actual center frequency \( f_{c,m}(n) \).

The accumulated displacement, \( u_m(n) \), is obtained by accumulating the estimated instantaneous displacement \( \Delta u_m(n) \) between 2 consecutive frames as follows:

\[ \dot{u}_m(n + 1) = \dot{u}_m(n) + \Delta u_m(n) \quad (u_m(0) = 0). \]  

(5)

Depth \( x_1(n) \) of the first point (luminal interface of the posterior wall) in the \( n \)th frame is determined by accumulated displacement \( \dot{u}_1(n) \) as follows:

\[ \dot{x}_1(n) = x_1(0) + \dot{D}(n) \cdot \Delta X, \]  

(6)

where \( \dot{D}(n) \) is an integer that satisfies \( \min \rho(n) \left| \dot{u}_1(n) - D(n) \cdot \Delta X \right| \) because the position of a correlation window is set depending on the spacing of the sampled points. For other points \( \{m\} \), their depths \( \{x_m(n)\} \) in the \( n \)th frame are determined by (1).

B. Modified Method for Estimation of Displacement Distribution

Fig. 2(a) shows a B-mode image of the phantom used in this study. The RF echo along the white vertical line in Fig. 2(a) is shown in Fig. 2(b). As can be seen in Fig. 2(b), the center frequency is not constant along the ultrasonic beam. This change in center frequency does not occur due to the well-known frequency dependent attenuation of ultrasound because the center frequency in a deep region—region B in Fig. 2(b)—is higher than that in a shallow region (region A).

When a target contains multiple scatterers within the duration of an ultrasonic pulse, interference between echoes from these scatterers occurs. An ultrasonic pulse has a certain frequency bandwidth, and thus such interference could be one of the reasons for the apparent change in center frequency (see the appendix). This subsection describes the displacement estimation method proposed in this study for reduction of the influence of center frequency variation.

The modified method comprises 2 main procedures: 1) estimation of displacement distribution in the arterial wall with tracking of the global motion of the arterial wall and 2) error reduction of the estimated displacement distribution using a newly proposed function.

1. Estimation of Displacement Distribution in Arterial Wall with Tracking of Global Motion: In conventional phase-sensitive correlation methods, the center frequency distributions in 2 different frames are assumed to be the same. Therefore, it is desired that the frame rate be as high as possible so that the deformation of the arterial wall becomes negligible, and thus the displacement should be estimated for every 2 consecutive frames.

On the other hand, the modified method does not require the above assumption. Therefore, the displacement distribution in the arterial wall need not be estimated for every 2 consecutive frames. Thus, several key frames are sparsely assigned, and the displacement distribution between 2 consecutive key frames is estimated. This procedure significantly reduces the number of calculations because the displacement of the arterial wall between 2 consecutive frames (4.2 μm) is smaller than the spacing of sampled points (19.25 μm), and thus there are multiple frames between 2 consecutive key frames, where the displacement of 4.2 μm is derived from the mean wall velocity of 1.2 mm/s during one cardiac cycle (measured in the carotid artery of a healthy subject) at a frame rate of 286 Hz. In this procedure, only the displacement at the luminal boundary is estimated using the conventional phase-sensitive correlation method described in Section II-A for every 2 consecutive frames so that the correlation window follows the position of the arterial wall (tracking of global motion).

Details of the above procedures are as follows: In this study, the global motion of the arterial wall is tracked using the displacement \( u_1(n) \) of the luminal boundary estimated by the conventional method described in Section II-A because the echo from the luminal interface is usually dominant in comparison with those from scatterers in the wall and is robust against interference. The displacement \( u_1(n) \) of echo from the luminal interface is estimated for every 2 frames at a high frame rate of 286 Hz. Therefore, the instantaneous displacement \( \Delta u_1(n) \) between 2 consecutive frames is less than the spacing \( \Delta X \) of the sampled points in the direction of depth \( x \).

Fig. 3 shows an example of the accumulated displacement \( u_1(n) \) at the luminal interface of the phantom used in this study. In this study, several key frames are defined as shown in Fig. 3. The frame number of the \( k \)th key frame is denoted by \( n_k \) and key frames are set so that the difference between the accumulated displacement \( u_1(n_k + 1) \) in the \((k + 1)\)th key frame and that \( u_1(n_k) \) in the \( k \)th key frame reaches spacing \( \Delta X \) of the sampled points. Then, the global motion of the wall is compensated by shifting the RF signal in the \((k + 1)\)th key frame by \( \Delta X \) of the sampled points before calculating the phase shift of RF echoes to obtain displacement \( \Delta u_{mn}(nk) \) between 2 consecutive key frames. This is done by setting lags \( n' \) and \( n'' \) in (3) to be \( \hat{D}(n_{k+1}) - \hat{D}(n_k) \) and \( n_{k+1} - n_k \), respectively, as follows:
where $|\hat{D}(n_{k+1}) - \hat{D}(n_k)| = 1$. The depth positions of correlation windows in the $k$th and $(k+1)$th key frames in (7) are different, whereas those in (4) are the same. This difference in the window positions corresponds to the compensation of global motion between these 2 key frames as shown in Fig. 4. Accumulated displacement $u_m(n_k)$ at depth $z_m(n_k)$ in the $k$th key frame is obtained by accumulation of the instantaneous displacement $\Delta u_m(n_k)$ during the period between 2 consecutive key frames as in (5).

$$\Delta u_m(n_k) = \frac{c_0}{4\pi f_{dem}} \Delta_{r_{mn}}(\hat{D}(n_{k+1}) - \hat{D}(n_k), n_{k+1} - n_k),$$

(7)

In this procedure, it is only necessary to calculate the displacement $u_1(n)$ at the luminal interface for every 2 consecutive frames ($n$th and $(n+1)$th frames). For other points $\{m\}$, displacements $\{u_m(n_k)\}$ are calculated for every 2 consecutive key frames. This procedure significantly reduces the number of computations because there are multiple frames between 2 consecutive key frames.

2. Error Correcting Function: In the conventional method described in Section II-A, the frequency $f_{dem}$ of the reference sinusoid in the quadrature demodulation is used

$$\hat{u}_m(n_k+1) = \hat{u}_m(n_k) + \Delta u_m(n_k) \quad (u_m(0) = 0).$$

(8)
instead of the actual center frequency \( f_{c,m}(n) \), as shown in (4), to estimate the displacement \( \Delta u_{m}(n) \). This assumption is also used in the modified method shown by (7). However, \( f_{dem} \) does not often match the actual center frequency \( f_{c,m}(n) \) of the RF echo. Loupas et al. proposed a method for estimating the mean frequency, \( \bar{f}_{c,m}(n) \), of the RF echo at each depth \( x_{m}(n) \) in frame \( n \) [43]. In the method described in [43], [44], the estimated mean frequency \( \bar{f}_{c,m}(n) \) is used in (4) instead of the demodulation frequency \( f_{dem} \) to obtain an unbiased displacement estimate. The mean frequency, \( \bar{f}_{c,m}(n) \), at the \( m \)th point in the \( n \)th frame is estimated as follows:

\[
\bar{f}_{c,m}(n) = f_{dem} - \frac{\mathcal{R}_{1,0}(1,0)}{2\pi T_s},
\]

where \( T_s \) is the sampling interval of the demodulated signal. By assuming that the mean frequency distributions \( \{\bar{f}_{c,m}(n)\} \) \( (m = 1, 2, \ldots, MT) \) in 2 consecutive frames are the same, the mean frequency distributions \( \{\bar{f}_{c,m}(n)\} \) estimated by (9) are used in the estimation of instantaneous displacements \( \{\Delta u_{m}(n)\} \) \((m = 1, 2, \ldots, MT)\) between 2 consecutive frames.

Fig. 5(a) shows RF echoes from the phantom used in this study (the same as in Fig. 2) in 2 consecutive frames. The frame interval is 3.5 ms (= 1/286 Hz). Fig. 5(b) shows the ratio of the mean frequency \( \bar{f}_{c,m}(n) \) estimated by (9) — \( M_c \) in (3) was set to 20 — to the demodulation frequency \( f_{dem} \) of 6.5 MHz. There is a difference in the mean frequency distributions \( \{\bar{f}_{c,m}(n)\} \) in 2 consecutive frames even though a high frame rate of 286 Hz was employed in this study.

Figs. 6(a) and 6(b) show RF echoes and mean frequency distributions estimated by (9) in 2 consecutive key frames. The interval between these 2 key frames is 69.9 ms. As shown in Fig. 6(b), there is a difference between the mean frequency distributions in 2 key frames. This difference is larger than that between 2 consecutive frames (3.5 ms) due to a longer frame interval.

In this study, an error correcting function, which does not require the assumption that the center frequency distributions in 2 different frames are the same, is introduced as follows: Let us consider the correlation functions
The absolute difference \( \Delta d_m(n_k) \) between the displacements given by \( \hat{r}_{0, n_k}(0, n_{k+1} - n_k) \) and \( \hat{r}_{m, n_k}(0, n_{k+1} - n_k) \) by substituting them into (4) instead of \( \hat{r}_{r_m}(0,1) \) should be the spacing of sampled points \( \Delta X \) because \( |\hat{D}(n_{k+1}) - \hat{D}(n_k)| = 1 \), i.e., the difference between the displacement estimated by the phase change of RF echo, which corresponds to \( \hat{D}(n_{k+1}) - \hat{D}(n_k) \), and the true displacement (corresponding to \( \Delta X \)) is evaluated. Thus, the ratio \( \gamma_m(n_k) \) of the estimated displacement difference \( \hat{D}(n_{k+1}) - \hat{D}(n_k) \) to the true displacement difference (= \( \Delta X \)) between the \( k \)-th and \( (k + 1) \)-th key frames is obtained as follows:

\[
\gamma_m(n_k) = \frac{c_0}{4\pi f_{dem} \Delta X} \left[ \hat{r}_{m, n_k}(0, n_{k+1} - n_k) - \hat{r}_{r_m}(0, n_{k+1} - n_k) \right].
\]  

By defining \( f_s \) as the sampling frequency of the demodulated signal, the numerator of (10) can be modified using the relation \( \Delta X = c_0/(2f_s) \) as follows:

\[
\gamma_m(n_k) = \frac{c_0}{4\pi f_{dem} f_s} \left| \hat{r}_{m, n_k}(0, n_{k+1} - n_k) - \hat{r}_{r_m}(0, n_{k+1} - n_k) \right|.
\]

Fig. 6(c) illustrates an example of the error correcting function \( \gamma_m(n_k) \) for the RF signals shown in Fig. 6(a).

The error corrected displacement, \( \hat{u}_m(n_k) \), is obtained by using \( \gamma_m(n_k) \) as the error correcting function as follows:

\[
\hat{u}_m(n_k) = \frac{1}{\gamma_m(n_k) \cdot 4\pi f_{dem}} \left( \Delta \hat{r}_{m, n_k}(0, n_{k+1} - n_k) - \hat{r}_{r_m}(0, n_{k+1} - n_k) \right).
\]

C. Estimation of Radial Strain from the Displacement Distribution

Fig. 7(a) shows an example of a received RF echo. Fig. 7(b) shows an example of the estimated accumulated displacement, \( \hat{u}_m \), at each sampled point \( m \) along an ultrasonic beam. Radial strain is obtained by estimating the regional slope of the displacement distribution \( \{ u_m \} \) (\( m = 1, 2, \ldots, M \)). The regional slope, \( \varepsilon_{r,m} \), around the \( m \)-th sampled point (depth \( x_m \)) is estimated by minimizing the mean squared difference, \( \alpha_m \), between the measured regional displacements \( \{ \hat{u}_m \} \) and the linear model, \( U_m = \varepsilon_{r,m} \cdot x + b_m \), as follows:

\[
\alpha_m = \frac{1}{M} \sum_{j=1}^{M} \left| \hat{u}_{m+j} - \varepsilon_{r,m} \cdot x + b_m \right|^2 \quad (m \leq M) \text{ and } (M + 1) \text{ layers overlap at the } m \text{th sampled point because the layer thickness } M \Delta X \text{ is greater than the interval } \Delta X \text{ of the sampled points. Thus, the compounded}
radial strain, $\varepsilon_{r,m}$ [45], at the $m$th sampled point is obtained by simply averaging the estimated regional slopes $\varepsilon_{r,m}$ of the layers, which overlap at the $m$th point as follows:

$$
\varepsilon_{r,m} = \begin{cases} 
\frac{1}{L_m} \sum_{j=1}^{M_s} \varepsilon_{r,m-j+1} & (m \leq M_T - M_s), \\
\frac{1}{L_m} \sum_{j=1}^{M_s} \varepsilon_{r,M_T-M_s-j+1} & (m > M_T - M_s), 
\end{cases}
$$

(14)

where $L_m$ is the number of overlapping layers at the $m$th point.

As shown in Fig. 7(a), a dominant echo from the luminal interface is found in the period from 0 to about 0.13 $\mu$s. The phase shift of sampled points within this echo corresponds to the displacement of the luminal interface. Therefore, a constant displacement is found during the duration of that echo as shown by the region surrounded by the dashed line in Fig. 7(b). As a result, strain is hardly detected during that period (from 0 to 0.13 $\mu$s) when the width $M_s$ for estimation of the regional slope in (13) is less than the pulse duration. However, such a decrease in the estimated strain is just an artifact due to the finite pulse duration. To reduce this artifact, in this study, the width used for estimating the regional slope $\varepsilon_{r,m}$ was set to be longer than the duration of the employed ultrasonic pulse.

### III. Materials and Methods

In this study, a cylindrical phantom and an excised artery were measured by ultrasound. The outer and inner diameters of the phantom, made of silicone rubber, were 10 and 8 mm, respectively. The phantom contained 5% carbon powder (by weight) to obtain sufficient scattering from inside the wall.

Fig. 8 shows a schematic diagram of the measurement system. A change in pressure inside the phantom or artery was induced by circulating a fluid using a flow pump. The change in internal pressure was measured by a pressure sensor (9E02-P16, NEC, Tokyo, Japan).

In ultrasonic measurement, the phantom and artery were measured with a linear-type ultrasonic probe (SSD-6500, Aloka, Tokyo, Japan). The nominal center frequency was 10 MHz. RF echoes were acquired at 40 MHz at a frame rate of 286 Hz.

Pressure-diameter testing was applied to the phantom to obtain the elastic modulus of silicone rubber. In the pressure-diameter testing, the change in external diameter of the phantom was measured with a laser line gauge (VG-035, KEYENCE, Osaka, Japan).

In the in vitro experiment, a femoral artery excised from a patient with arteriosclerosis obliterans was measured. The artery was placed in a water tank filled with 0.9% saline solution at room temperature. A needle was attached to the external surface of the posterior wall using strings to identify the sections to be imaged during the ultrasonic measurement. After the ultrasonic measurement, pathological images of the measured sections were obtained with reference to the needle.

### IV. Basic Experimental Results

#### A. Pressure-Diameter Testing of the Phantom

Fig. 9(a) shows the trigger signal for driving the flow pump. Figs. 9(b) and 9(c) show waveforms of the internal pressure and change in the external diameter of the phantom, respectively. In Fig. 9, the waveforms of 10 measurements are superimposed. From the measured internal pressure, $p_i$, and the change in external diameter, $2 \cdot \Delta r_i$, the elastic modulus, $E$, is obtained as follows [46]:
where \( r_i \) and \( r_o \) are the original internal and external radii, respectively.

In Fig. 9(d), the measured internal pressure \( p_i \) is plotted as a function of the change in external diameter \( 2\Delta r_o \). The slope, \( p_i/\Delta r_o \), was estimated by applying the least-squares method to the measured data shown in Fig. 9(d). The estimated slope \( p_i/\Delta r_o \) is shown by the solid line in Fig. 9(d). The elastic modulus \( E \) of the phantom was determined to be 749 kPa.

**B. Ultrasonic Measurements of the Phantom**

1. **Comparison of Conventional and Proposed Methods:**

The radial strain distribution inside the wall of the phantom was estimated by the conventional phase-sensitive correlation method described in Section II-A, as shown in Fig. 10(a). The length of the correlation window determined by \( M_c \) and that for estimating strain determined by \( M_s \) are set to 0.5 \( \mu s \) (corresponding to the length at \(-20\) dB of the maximum magnitude of the quadrature demodulated signal of the ultrasonic pulse, \( M_c = 20 \)) and 1.0 \( \mu s \) (twice the length at \(-20\) dB, \( M_s = 40 \)), respectively, for both the conventional and proposed methods. In Fig. 10(a), plots and vertical bars show the means and standard deviations of the radial strain in the radial direction (along the ultrasonic beam). The mean value and standard deviation at each radial position are obtained by the individual strain distributions along 46 ultrasonic beams. The solid curve in Fig. 10(a) shows the theoretical radial strain \( \varepsilon_r \) of a homogeneous tube at each radial position \( r \), which is obtained using the elastic modulus \( E \) measured by pressure-diameter testing and the measured internal pressure as follows [46]:

\[
\varepsilon_r = \frac{3}{2} \frac{r_i^2}{(r_o^2 - r_i^2)} \frac{p_i}{r_o^2 - r_i^2} \frac{2}{\Delta r_o} E.
\]

In Fig. 10(a), mean values tend to follow the theoretical profile. However, the standard deviation is large. Mean error \( e_{\text{mean}} \) and standard deviation \( \text{SD}_{\text{mean}} \) evaluated by (17) and (18) were 23.7% and 46.2%, respectively.

\[
e_{\text{mean}} = \frac{1}{M_T} \sum_{m=1}^{M_T} \left| \varepsilon_r^{m} - \varepsilon_r^{m, \text{mean}} \right|,
\]

\[
\text{SD}_{\text{mean}} = \frac{1}{M_T} \sum_{m=1}^{M_T} \sqrt{\frac{1}{M_T} \sum_{m=1}^{M_T} \left( \varepsilon_r^{m} - \varepsilon_r^{m, \text{mean}} \right)^2},
\]

where \( E_{[\cdot]} \) represents the averaging with respect to the beam position \( i \).

Fig. 10(b) shows the strain distribution obtained by the conventional phase-sensitive correlation method with mean frequency estimation (Loupas’s method) [43]. There is no distinct improvement in the strain estimates. The strain distribution obtained by Loupas’s method with spatial compounding [45] shown in Fig. 10(c) is in good agreement with the theoretical strain profile, and the standard deviation is significantly reduced. Note that vertical scales in Figs. 10(c) and 10(d) are different from those in Figs. 10(a) and 10(b).

Fig. 10(d) shows the radial strain distribution obtained by the method proposed in this study. The difference between the mean values and the theoretical profile shown by the solid curve was further reduced, but the standard deviation was similar to that obtained by Loupas’s method with spatial compounding. From this result, it can be said that the variance was reduced mainly by the spatial compounding. Mean error \( e_{\text{mean}} \) and standard deviation \( \text{SD}_{\text{mean}} \) of the strain distribution estimated by the proposed method were \( e_{\text{mean}} = 12.0\% \) and \( \text{SD}_{\text{mean}} = 14.1\% \), respectively.
2. Consideration of the Size of Correlation Window and Period for Estimating Strain:

Fig. 11(a) shows error $e_{\text{mean}}$ in the strain distribution of the phantom estimated by the proposed method at each combination of the period for estimating strain and the length of the correlation window. As shown in Fig. 11, error $e_{\text{mean}}$ is reduced by lengthening the period for estimating strain, and this effect of error reduction is almost complete at 1.0 μs ($M_s = 40$ in (13)).

Fig. 11(b) shows the error distribution at the period for estimating strain of 1.0 μs. The strain estimates are not much influenced by the correlation window length in comparison with the period for strain estimation, and the error reduction is almost complete at the correlation window lengths of 0.5 μs. Therefore, the length of 0.5 μs ($M_c = 20$ in (3) and (7)) was selected to achieve a better spatial resolution, whereas the error at 0.6 μs is slightly smaller. The correlation window length of 0.5 μs ($M_c = 20$) and the period for estimating strain of 1.0 μs ($M_s = 40$) correspond to the length at −20 dB of the maximum magnitude of the quadrature demodulated signal of the ultrasonic pulse and twice that length, respectively.

V. In Vitro Experimental Results

Figs. 12(a-1) and 12(b-1) show the B-mode images of 2 different regions in the excised femoral artery. The region shown in Fig. 12(a-2) shows very low strain. On the other hand, the region shown in Fig. 12(b-2) shows relatively larger strain, and there is a clear strain decay with respect to the distance from the lumen [46]. Figs. 12(a-3) and 12(b-3) show the elasticity images obtained by (16) using the measured internal pressure and estimated strain distributions. By comparing the elasticity images and pathological images of the corresponding sections shown in Figs. 12(a-4), 12(b-4), 12(a-5), and 12(b-5), the very hard region surrounded by the green line in Fig. 12(a-3) corresponds to calcified tissue. On the other hand, the region composed of smooth muscle and collagen shows a relatively homogeneous and lower elastic modulus dis-
distribution. These results show that the proposed method successfully reveals the difference in the deformation properties resulting from different tissue compositions.

VI. Discussion

In the method proposed in this study, the interval of frames between which the phase shift of echoes is estimated was increased to reduce the number of computations. However, aliasing does not occur because the large global motion is tracked (compensated) by the conventional method at a high frame rate of 286 Hz. The global motion between 2 key frames is the distance corresponding to an interval of sampled points, 19.25 μm in this study (speed of sound: 1,540 m/s). Therefore, the residual displacements at other radial positions after global motion compensation are less than 19.25 μm after global motion compensation. When the center frequency of the received RF echo is exactly the same as the nominal center frequency (10 MHz) of the employed ultrasonic probe, a displacement of 19.25 μm produces a phase shift of RF echoes of π/2. The residual displacement at each radial position after global motion compensation is smaller than 19.25 μm, which is smaller than the aliasing limit of 38.5 μm at 10 MHz.

The proposed method does not remove the global motion perfectly because the displacement at the luminal interface estimated by the conventional phase-sensitive correlation method is used to compensate for the global motion, and, in usual cases, the frequency of the reference sinusoid used in the quadrature demodulation does not exactly match the center frequency of the RF echo from the luminal interface. However, even in such situations, the proposed method can compensate for most of the global motion, and it is one of the simplest ways to track the global motion.

On the other hand, by using companding to find the exact match between the precompression and postcompression RF signals [11], [12], [35]–[40], more accurate displacement estimates would be achieved because such methods do not require information on the center frequency and enable better correction of the difference between the center frequencies of 2 RF signals. In the present study, however, RF signals were sampled at a frequency only 4 times the transmit center frequency, whereas a higher sampling frequency (or interpolation) is desirable in such other methods. The objective of this study was to develop a method that can be applied to an RF signal sampled at a lower frequency with less computation but reasonable accuracy, and the scientific meaning of this study is the introduction of an error correcting function that reduces the influence of the center frequency variation on the displacement estimation without requirement of the assumption that the center frequency distributions in 2 different frames are the same.

As described above, in this study, improvement of the strain estimates by the proposed method was shown by basic experiments using a cylindrical phantom. The true
strain distribution in an actual arterial wall is difficult to know, particularly in the case of a diseased region, as shown in Fig. 12(a). Therefore, in this study, we just demonstrated that the strain and elasticity distributions estimated by the proposed method were in good agreement with the pathology. The usefulness of the proposed method in clinical situations should be further investigated by applying it to more arteries in in vitro and in vivo experiments.

Finally, in the estimation of the elastic modulus, determination of the stress distribution is a major problem. In this study, the stress distribution defined by (16) was used to obtain the elasticity images shown in Fig. 12(a-3) and 12(b-3). However, it agrees with the actual stress distribution only in the case of a homogeneous cylindrical shell. Such a difference between the actual stress distribution and that used in elasticity estimation leads to a significant error. Recently, several studies have been conducted to reconstruct elastic modulus distributions [47]–[49]. However, the method employed has not yet been applied to both longitudinal and cross-sectional scans of the arteries, and determination of the stress distribution remains an important problem in vascular elasticity imaging.

VII. Conclusions

In the displacement estimation based on the phase change of echoes, the displacement estimates are biased when the center frequency of the RF echo changes. Such an apparent change in the center frequency could be caused by the interference of echoes from scatterers. To reduce the influence of the center frequency variation on the estimation of artery-wall strain, in this study, an error correcting function, which does not require the assumption that the center frequency distributions in 2 different frames are the same, was introduced. As a result, the proposed method provides better strain estimates in comparison with conventional phase-sensitive correlation methods.

APPENDIX

Influences of Interference on Center Frequency

In the case of a target containing multiple scatterers, the interference between echoes from these scatterers occurs because there are multiple scatterers within the duration of an ultrasonic pulse. An ultrasonic pulse has a certain frequency bandwidth, and thus the interference of echoes could be one of the reasons for the change in center frequency.

Fig. 13(a-1) shows a simulated RF echo from a single point scatterer, and Fig. 13(a-2) shows its power spectrum. The center frequency is set to 7.5 MHz, and the envelope is a Hanning window with a length corresponding to 5 cycles of the center frequency. Figs. 13(b-1) and 13(c-1) show the RF echoes from 2 scatterers that exist along an ultrasonic beam. The spacings of scatterers in Figs. 13(b-1) and 13(c-1) are 162 μm and 240 μm, respectively. As shown in Figs. 13(a-2), 13(b-2), and 13(c-2), depending on the spacing of scatterers, even when there are only 2 scatterers, the dominant frequency changes in a complex way due to the interference of echoes.

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